

# ECON 815

## Fiscal Policy in the RBC Model

Winter 2014

## RBC Model with Policy Shocks

A *policy* is defined by

$$\{z_t\}_{t=0}^{\infty} = \{g_t, \tau_{ct}, \tau_{xt}, \tau_{kt}, \tau_{nt}, T_t\}_{t=0}^{\infty}$$

The policy is *feasible* if it satisfies a flow budget constraint

$$g_t = \tau_{ct}c_t + \tau_{xt}x_t + \tau_{kt}r_tk_t + \tau_{nt}w_tn_t - T_t$$

Public expenditures  $g$  do not provide direct utility.

There are no technology shocks, but we would like to look at *anticipated policy changes* and *unanticipated policy shocks*.

Households take prices and policy as given to maximize

$$\max_{\{c_t, n_t, x_t\}_{t=0}^{\infty}} \sum_{t=0}^{\infty} \beta^t u(c_t, 1 - n_t)$$

subject to

$$(1 + \tau_{ct})c_t + (1 + \tau_{xt})x_t \leq (1 - \tau_{kt})r_t k_t + (1 - \tau_{nt})w_t n_t + T_t$$

$$k_{t+1} = (1 - \delta)k_t + x_t$$

$k_0$  given

Firms have a neoclassical production function and, taking prices as given, maximize profits

$$r_t = F_k(k_t, n_t)$$

$$w_t = F_n(k_t, n_t)$$

# Tax Wedges

Intratemporal distortion

$$\frac{(1 - \tau_{nt})}{(1 + \tau_{ct})} = \frac{u_n(c_t, 1 - n_t)}{u_c(c_t, 1 - n_t)F_n(k_t, n_t)}$$

Intertemporal distortion

$$\frac{u_c(c_t, 1 - n_t)}{\beta u_c(c_{t+1}, 1 - n_{t+1})} = \frac{(1 + \tau_{ct})}{(1 + \tau_{ct+1})} \left[ (1 - \delta) \frac{(1 + \tau_{xt+1})}{(1 + \tau_{xt})} + F_k(k_{t+1}, n_{t+1}) \frac{(1 - \tau_{kt+1})}{(1 + \tau_{xt})} \right]$$

## Steady State

The steady state is given by the solution  $(c^{SS}, n^{SS}, k^{SS})$  to

$$1 = \beta \left[ (1 - \delta) + \frac{(1 - \tau_k)}{(1 + \tau_x)} F_k(k^{SS}, n^{SS}) \right]$$

$$\frac{u_c(c^{SS}, 1 - n^{SS})}{u_n(c^{SS}, 1 - n^{SS})} = \frac{(1 - \tau_n)}{(1 + \tau_c)} F_n(k^{SS}, n^{SS})$$

$$g + c^{SS} + \delta k^{SS} = F(k^{SS}, n^{SS})$$

Suppose  $u(c, 1 - n) = u(c)$ , i.e. labour is inelastically supplied. Then, taxing consumption is non-distortionary.

- ▶ labour taxes are lump-sum
- ▶ constant consumption taxes ( $\tau_c \neq 0$ ) are not distorting either
- ▶  $\tau_x = \tau_k = 0$  is optimal in steady state  $k^{SS}$

## Distortions in TFP vs. Policy

What accounts for persistent differences in countries GDP?

1) OECD vs. developing countries:

Different institutions are “barriers to riches” and lead to lower TFP.

2) Within OECD:

Labour taxes are higher in some countries leading – with high enough labor elasticity – to losses in GDP.

## Variations in Policy Matter

Denote the after-tax gross return on capital by  $R_{t+1}$  and assume CRRA utility function.

With inelastically supplies labour ( $n = 1$ ), we get

$$u'(c_t) = \beta u'(c_{t+1}) R_{t+1}$$

or

$$\log \left( \frac{c_{t+1}}{c_t} \right) = \frac{1}{\gamma} (\log \beta + \log R_{t+1}).$$

The return  $R_{t+1}$  – and, hence, investment and consumption – is influenced by *variations* in tax rates.

We will assume that changes in tax rates or expenditures are covered by corresponding changes in the lump-sum tax  $T$  (pure changes in distortions or expenditures).

## Policy Experiments

We look at announced policy changes in period 0 that will take effect in period  $T$ .

There is a response to the announcement. The economy will react before the shock happens based on rational expectations about future policy changes.

There is a transient response after the shock to go back to the (possibly new) steady state.

We still can distinguish between permanent and temporary policy changes.

Lump-sum transfers are always available to satisfy the government's budget constraint.

- ▶ take labour to be inelastically supplied
- ▶ explicitly we vary taxes or expenditures
- ▶ implicitly we need to adjust lump-sum transfers



# Experiment I – Surprise in $g$

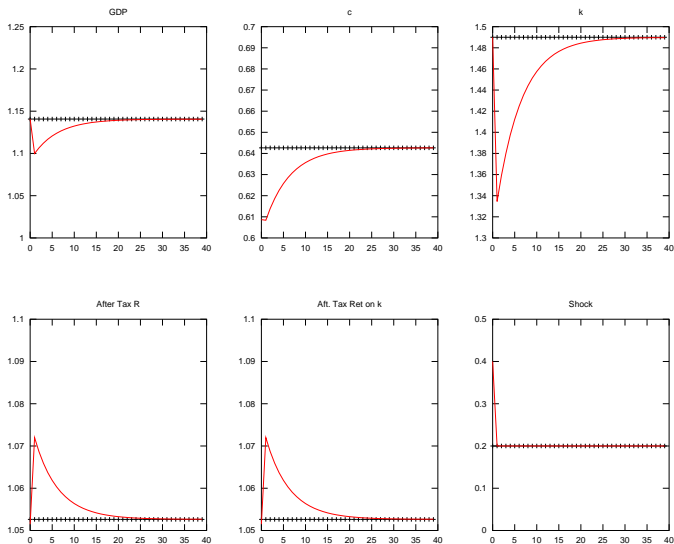


Figure: Temporary increase in  $t = 0$  from  $g = 0.2$  to  $g = 0.4$

# Experiment II – Announcement of increase in $g$

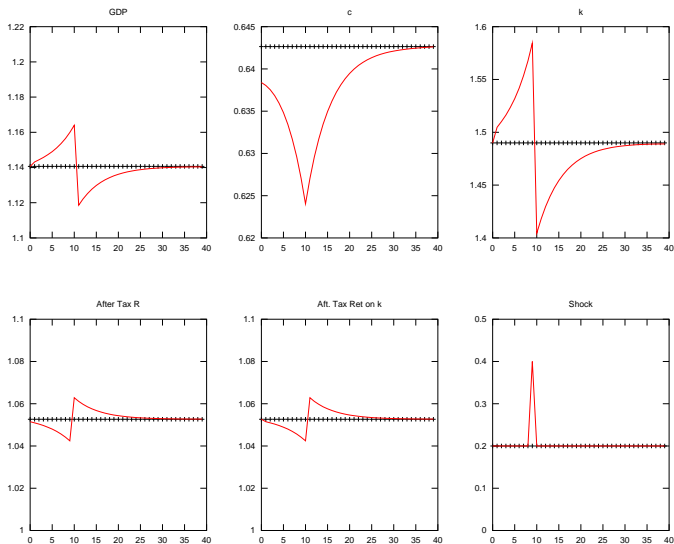


Figure: Temporary increase in  $t = 10$  from  $g = 0.2$  to  $g = 0.4$

# Experiment III – Announcement of increase in $g$

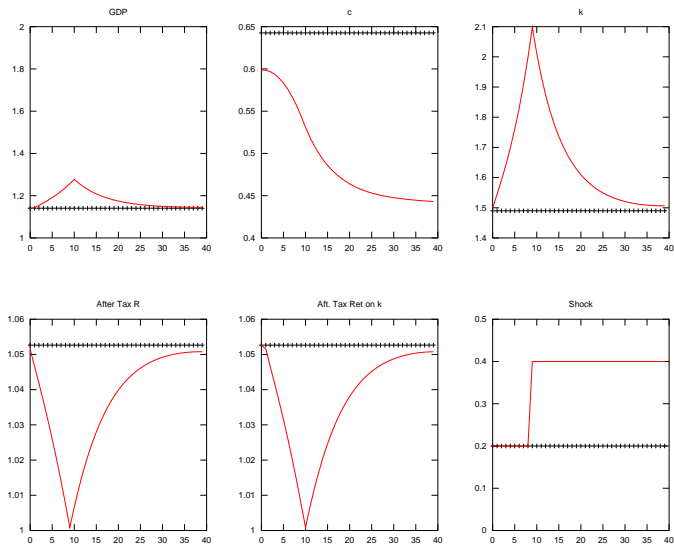


Figure: Permanent increase in  $t = 10$  from  $g = 0.2$  to  $g = 0.4$

# Experiment IV – Announcement of increase in $\tau_c$

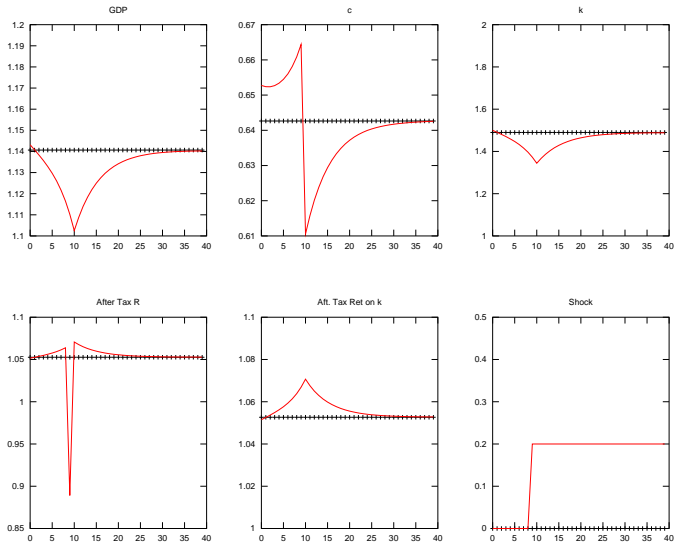


Figure: Permanent increase in  $t = 10$  from  $\tau_c = 0$  to  $\tau_c = 0.2$

# Experiment V – Announcement of increase in $\tau_i$

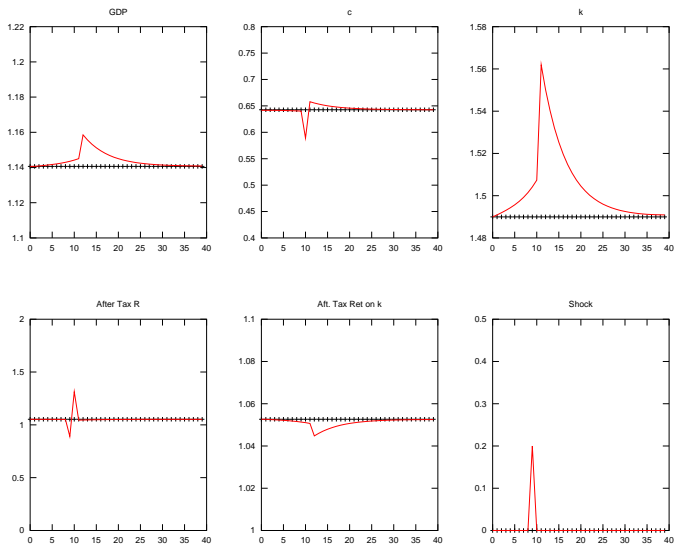


Figure: Temporary increase in  $t = 10$  from  $\tau_i = 0$  to  $\tau_i = 0.2$

# Experiment VI – Announcement of increase in $\tau_i$

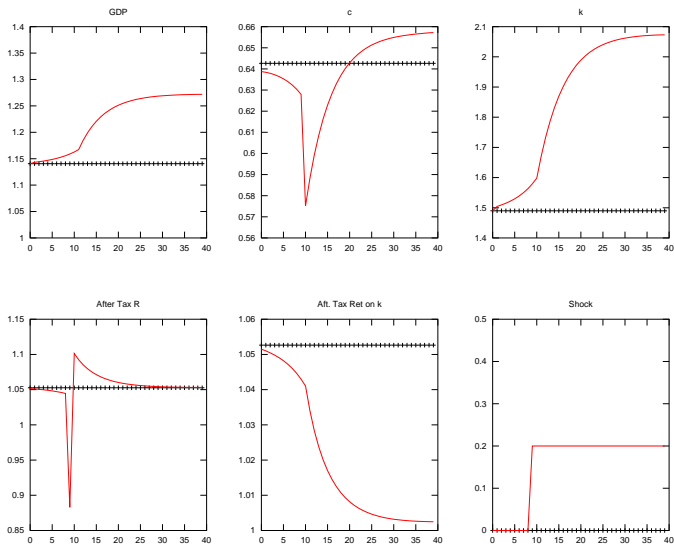


Figure: Permanent increase in  $t = 10$  from  $\tau_i = 0$  to  $\tau_i = 0.2$

# Experiment VII – Announcement of increase in $\tau_k$

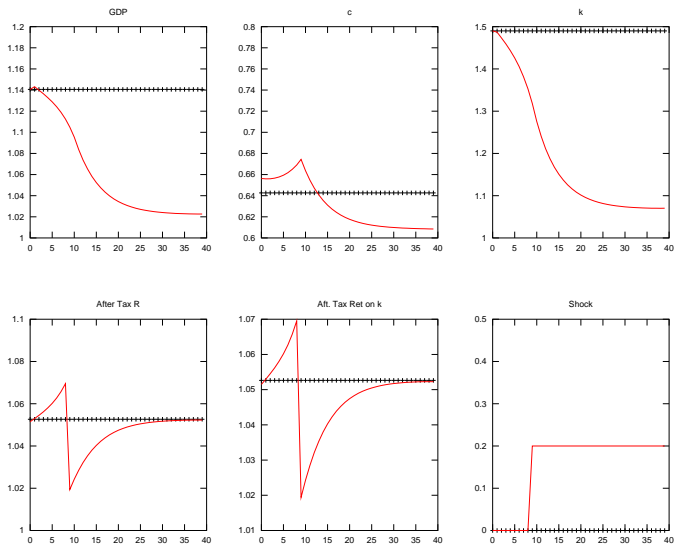


Figure: Permanent increase in  $t = 10$  from  $\tau_k = 0$  to  $\tau_k = 0.2$